MEMOCODE 2016 Design Contest:  
k-Means Clustering

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Abstract—K-means is a clustering algorithm that aims to  
group data into $k$ similar clusters. The objective of the 2016  
MEMOCODE Design Contest is to implement a system to  
efficiently partition a large set of multidimensional data using  
k-means. Contestants were given one month to develop a system  
to perform this operation, aiming to maximize performance or  
cost-adjusted performance. Teams were encouraged to consider  
a variety of computational targets including CPUs, FPGAs, and  
GPGPUs. The winning team, which was invited to contribute a  
paper describing their techniques, combined careful algorithmic  
and implementation optimizations using CPUs and GPUs.

I. INTRODUCTION

This year marks the tenth iteration of the annual MEM-  
OCODE design contest. Since 2007, contests have posed a  
variety of problems to teams from around the world, focusing  
on hardware/software solutions. Previous problems have  
included bioinformatics [1], simulation of NoCs [2], computer  
vision [3], data mining [4], [5], packet inspection [6],  
rectangular-to-polar interpolation [7], sorting of encrypted  
data [8], and matrix-matrix multiplication [9]. This year’s  
problem is to perform k-means clustering on a large data set.

II. OVERVIEW

Figure 1 illustrates a simple example performing k-means  
clustering on two-dimensional data. The black and blue squares  
represent the data we want to cluster, and the large red circles  
show the centers of our $k = 2$ clusters. Initially (Step 1),  
the cluster centers are randomly-generated; the squares are colored  
black or blue to indicate which of the two clusters each point  
belongs to. The black-colored points are those closest to the  
top-left center, and the blue-colored points are those closest to  
the bottom-right center.

We can easily see in Step 1 that our randomly-chosen  
centers are not well-placed with respect to the data. The algorithm proceeds by re-calculating the location of each  
center as the mean value of all the points within its cluster. That is, the top-left red circle’s location gets moved to the mean of the locations of all the black squares, and the bottom-right red circle’s location gets moved to the mean of the locations of all the blue squares.

The algorithm then proceeds iteratively. In the next iteration (Step 2), the same sequence of operations are performed. First, each of the data points is compared with the locations of the centers, and is assigned to the closest cluster. Then, the centers’ locations are again updated by averaging the locations of each element in the cluster.

As each iteration proceeds, the centers will move to better  
cluster the data. We can see that by Step 3 the blue and black dots are becoming better separated; by Step 4 they are fully separated. The iterative algorithm will repeat until it converges or a fixed number of iterations is reached.

Problem Description. Let $D$ represent a set of observations consisting of $n$ elements $d_0, \ldots, d_{n-1}$, each representing a point in $m$-dimensional space. Our goal is to partition these $n$ points into $k$ clusters $S_0, \ldots, S_{k-1}$ in a way that minimizes the distances between each element in $D$ and the center of its nearest cluster.

That is, the goal is to partition $D$ into $k$ clusters $S_t$ that minimizes

$$
\sum_{i=0}^{k-1} \sum_{d \in S_i} ||d - \mu_i||^2,
$$

where $\mu_i$ is the center (average) of all points assigned to  
cluster $S_i$, and distance is quantified using squared-Euclidean
where $a_i$ and $b_i$ represent the $i$-th dimension of the $m$-dimensional $a$ and $b$ vectors. Note that we use squared Euclidean distance to avoid an unnecessary square-root operation.

**Heuristic Algorithm.** A common method for performing this clustering is an iterative refinement technique commonly known as Lloyd’s algorithm [10]. Given a set of $k$ initial cluster centers $\mu_0, \ldots, \mu_{k-1}$, each iteration performs the following two steps:

1) **Assignment:** assign each $d_j$ in $D$ to the cluster $S_i$ whose center $\mu_i$ is closest to it (based on the squared Euclidean distance).
2) **Update:** Calculate the new centers $\mu_i$ of each cluster $S_i$ as the average location of all points in $S_i$:

$$\mu_i = \frac{\sum_{d_i \in S_i} d_j}{|S_i|},$$

where $|S_i|$ represents the number of elements assigned to $S_i$.

These two steps repeat until the algorithm converges or a fixed number of iterations is reached. For this contest, we target a fixed number of iterations of Lloyd’s algorithm, or an equivalent distance-metric target if other algorithms are used.

**III. Problem Specification**

The goal of the contest is to define a system that takes as input: (1) a data set $D$ consisting of $n$ points in $m$ dimensions (where $n$ and $m$ are given), (2) a set of $k$ locations (randomly-chosen) in $m$-dimensional space which will serve as the initial locations to place the cluster centers $\mu_i$, and (3) the number of iterations to perform if using Lloyd’s algorithm (or the target cost metric if using another algorithm).

The system will produce as output: (1) the label for each of the $n$ points (each is an integer between 0 and $k-1$ inclusive), and (2) the final $k$ cluster centers in $m$-dimensional space.

The timed portion of the solution must start with all input data in main system memory, and it must conclude with all output data in main memory.

**Algorithm Choice and Clustering Accuracy.** Different algorithms for performing this clustering can result in differing numbers of iterations (i.e., a given algorithm may reach the same quality of results in fewer iterations), or they may converge on a different local minimum. For this reason, we allowed any algorithm to be used so long as it reached a solution “as good” as the naive reference algorithm, as measured by the sum of the squared Euclidean distances of each the point from its nearest center:

$$\text{total distance} = \sum_{i=0}^{k-1} \sum_{d \in S_i} \|d - \mu_i\|^2,$$

where $\mu_i$ is the center (average) of all points assigned to cluster $S_i$, and $\|a - b\|^2$ is defined as in (1).

A target distance computed using this metric was provided to contestants with the reference data sets.

**Datatype.** Elements in $D$ were given as signed integers. The range of the input values was limited such that every input element can be represented as a 16-bit signed value.

The final output values are: (1) the labels of each input element in $D$ (thus, unsigned integers between 0 and $k-1$), and (2) the set of $k$ cluster centers in $m$-dimensional space (where each is a signed integer value).

Designers were allowed to choose to optimize the datatype as appropriate. There was no constraint on the order that the results were reported; for convenience the reference implementation code sorts them before storing to a file. (The time for this operation was not included in our timing measurements.)

**Functional Reference Implementation.** We provided an unoptimized naive software implementation of Lloyd’s algorithm to serve as the functional reference for the contestants’ optimized implementations. It computes the given number of iterations and stores the result.

This is summarized by the following pseudocode, given $k$ clusters, $m$ dimensions, and $T$ iterations.

```plaintext
initialize;
// begin timing here
for t = 1 to T {
    for i = 1 to data set size {
        minDist = LONG_MAX;
        for j = 1 to k {
            dist = calcDist(data[i], cluster[j])
            if (dist < minDist) {
                minDist = dist
                labels[i] = j
            }
        }
        clusterSums[labels[i]] += data[i]
        clusterCounts[labels[i]]++
    }
    for j = 1 to k {
        centers[j] = clusterSums[j]/clusterCounts[j]
    }
// end timing here
sort and output results;
```

Based on the problem definition, the order of the output values does not matter. For convenience, the functional reference code performs post-processing to sort results based on their location; this was done to allow an easy use of `diff` to determine if two output files are equivalent. This sorting was not required to be in contestants’ implementations, and its runtime was ignored.

**Data sets.** Three data sets were provided to aid in validation and development. Each set contains an $m$-dimensional input data set $D$ and the initial values of the center locations. Each set is accompanied by a reference solution (computed using Lloyd’s algorithm) that provides the sorted center locations and accompanying labels for each input value. Details of
the test data are given in Table I. All test data were generated synthetically to have the desired size and characteristics.

IV. THE CONTEST

Participants were given approximately one month to implement a solution using platforms such as FPGAs, GPUs, and CPUs. The solutions were validated using the supplied reference data sets. Performance was measured using the large data set. The time taken to initialize data and to sort and read the final result from memory was excluded from the runtime measurement.

The submitted solutions were evaluated using two metrics: pure performance and cost-adjusted performance. The pure-performance metric was based solely on runtime, while the cost-adjusted metric was defined as the product of runtime and system cost. The system cost was determined based on the lowest listed commercial price; if no price were available, the system cost would be estimated by the judges. Contestants were encouraged to include their own estimate of system cost with their submissions.

V. RESULTS

In order to access the reference code and data, contestants were asked to register by e-mail. Five teams consisting of members from five different countries registered; only one team submitted a full working implementation. This submission targeted GPUs and CPUs.

Table II summarizes the submitted results on several platforms. The names and full affiliations of the participants are included at the end of the paper.

As shown in the table, the winning team, from the Institute for Research in Fundamental Sciences (IPM), Iran, implemented their design using Intel Xeon E5 CPUs and NVIDIA GTX 980 GPUs. Their overall best result computed the solution in 106ms using four GPUs. In terms of cost-normalized results, their best solution was the 2x GPU implementation, which was only 1.5x slower than the 4x GPU solution, at half the cost. The IPM team’s implementation strategy involved careful parallelization of the problem across available platforms, as well as optimization of the arithmetic required by the problem. Their solution was based on Lloyd’s algorithm, and they have contributed an invited paper to these proceedings detailing their techniques [11].

VI. CONCLUSION

The 2016 MEMOCODE Design Contest was to efficiently compute k-means clustering on a large multidimensional data set. The winning team performed effective optimizations involving the algorithmic structure and parallelism.

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Thanks to all of the contestants for their hard work, and we congratulate our winners on their excellent results. Thank you also to Yi Deng, Elizabeth Leonard, Klaus Schneider, Sandeep Shukla, and Jean-Pierre Talpin for their help in planning and organizing this contest.

PARTICIPANTS

Thank you to all of the participants. The winning team’s members are Saeid Rahmani, Armin Ahmadzadeh, Omid Hajihassani, SeyedPooya Mirhosseini, and Saeid Gorgin, from Institute for Research in Fundamental Sciences (IPM), Iran.

REFERENCES